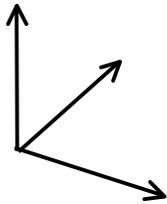


Tonight's Agenda

- 1) Quick review of last week
- 2) Lesson on Force and Motion
- 3) Experiments on Force and Motion
- 4) More discussion on Post Project
- 5) Volunteers for Holiday Party

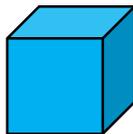
Basic Quantities - Independent



Space - Length



Time



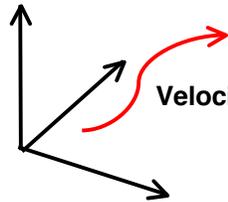
Matter - Mass



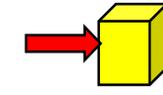
Charge - Electro-magnetics

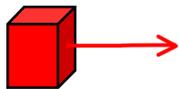
Derived Quantities

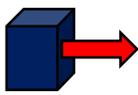
Combinations of Basics

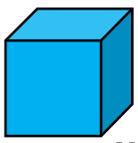

$$\text{Velocity} = \frac{\text{Length}}{\text{Time}}$$

**Dimensionality
And Units**


$$\text{Force} = \frac{\text{Mass Length}}{\text{Time}^2}$$


$$\text{Momentum} = \frac{\text{Mass Length}}{\text{Time}}$$


$$\text{Energy} = \frac{\text{Mass Length}^2}{\text{Time}^2}$$


$$\text{Density} = \frac{\text{Mass}}{\text{Length}^3}$$

Derived Quantities

Used in Aerodynamics

$$\text{Density} = \frac{\text{Mass}}{\text{Length}^3}$$

$$\text{Force} = \frac{\text{Mass Length}}{\text{Time}^2}$$

$$\text{Velocity} = \frac{\text{Length}}{\text{Time}}$$

$$\text{Momentum} = \frac{\text{Mass Length}}{\text{Time}}$$

$$\text{Pressure} = \frac{\text{Force}}{\text{Area}} = \frac{\text{Mass}}{\text{Length Time}^2}$$

$$\text{Energy} = \frac{\text{Mass Length}^2}{\text{Time}^2}$$

$$\text{Torque} = \frac{\text{Mass Length}^2}{\text{Time}^2}$$

$$\text{Mass Flow} = \frac{\text{Mass}}{\text{Time}}$$

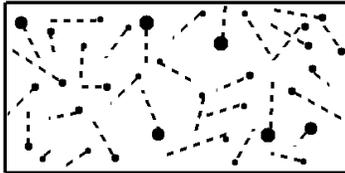
Dimensionality

Temperature – Basic or Derived ?



Kinetic Theory of Gases

Glenn
Research
Center



Molecular Model: Small molecules relative to distance apart.
Molecules in constant random motion.
Frequent collisions between molecules.
Ordered motion superimposed on random motion.

Density -> mass and volume

Pressure -> momentum (mass x velocity)

Temperature -> kinetic energy (mass x velocity²)

Laws of Physics ?

Observations of the Relations between Derived Quantities



Newton's Laws of Motion

Glenn
Research
Center



"Every object persists in its state of rest or uniform motion in a straight line unless it is compelled to change that state by forces impressed on it."

"Force is equal to the change in momentum (mv) per change in time. For a constant mass, force equals mass times acceleration."
 $F = m a$

"For every action, there is an equal and opposite re-action."

Tonight's Agenda

- 1) Quick review of last week**
- 2) Lesson on Force and Motion**
- 3) Experiments on Force and Motion**
- 4) More discussion on Post Project**
- 5) Volunteers for Holiday Party**



*Glenn
Research
Center*

Forces and Motion

Tom Benson
Thomas.J.Benson@nasa.gov

How do I describe the location of an object ?



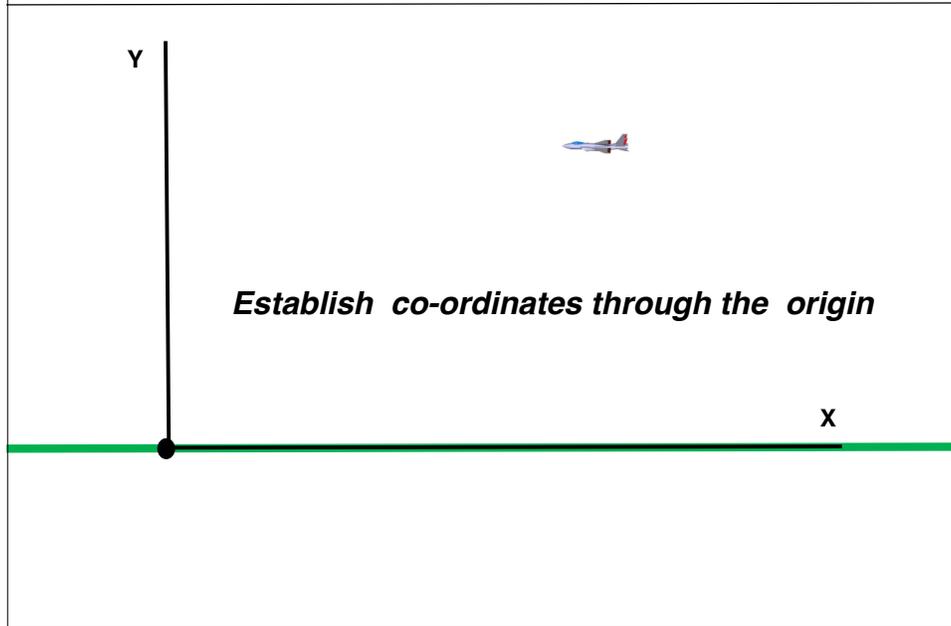
How do I describe the location of an object ?



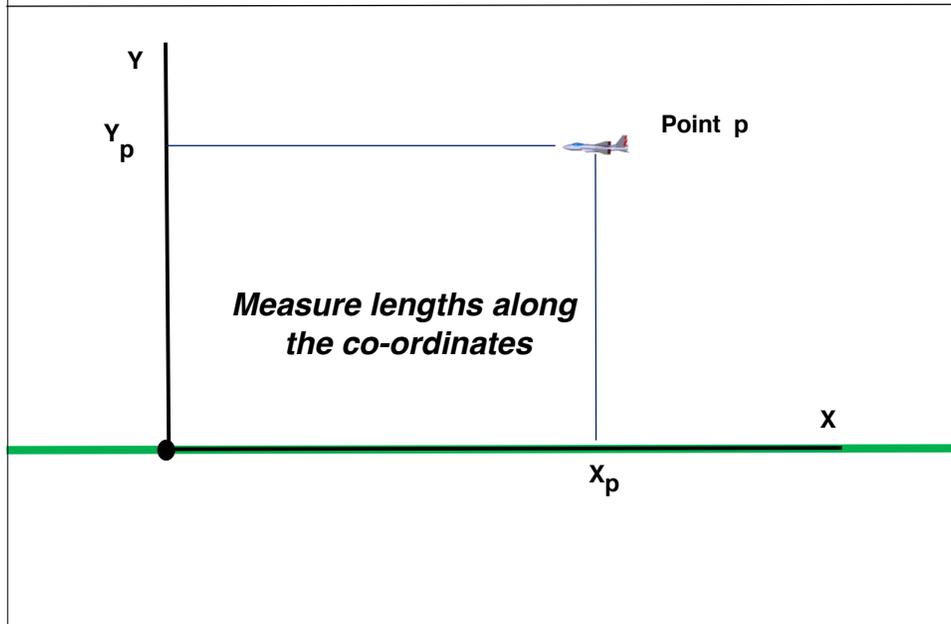
Select an Origin - point of reference



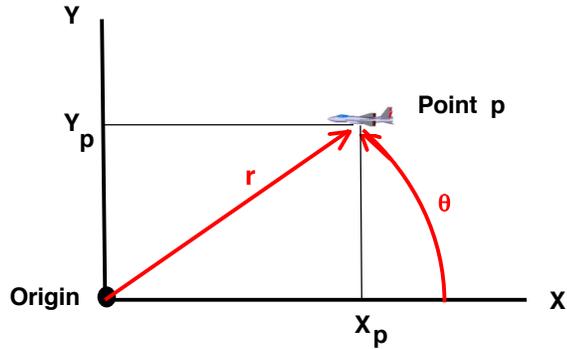
How do I describe the location of an object ?



How do I describe the location of an object ?



Rectangular and Polar Coordinates



Point p can be located relative to the origin by Rectangular Coordinates (X_p, Y_p) or by Polar Coordinates (r, θ)

$$X_p = r \cos(\theta)$$

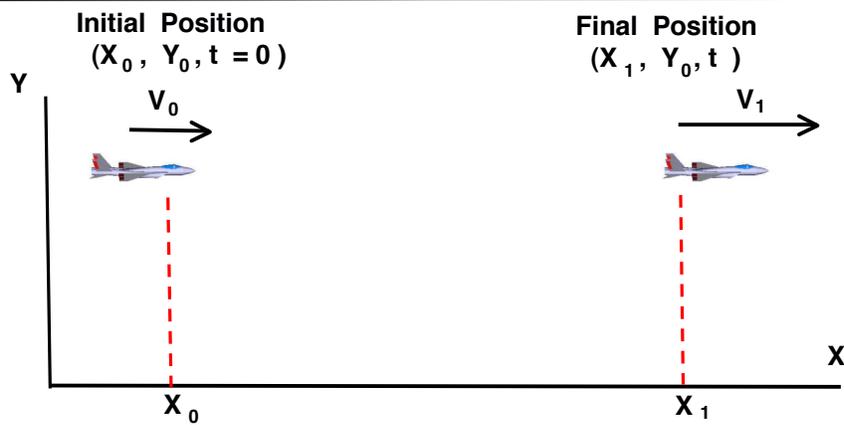
$$r = \sqrt{X_p^2 + Y_p^2}$$

$$Y_p = r \sin(\theta)$$

$$\theta = \tan^{-1}(Y_p / X_p)$$

13

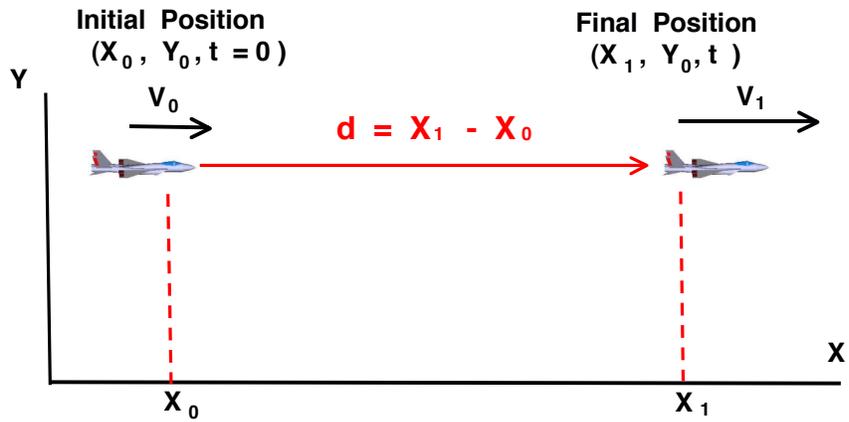
Suppose the Object Moves?



How do we describe the motion?

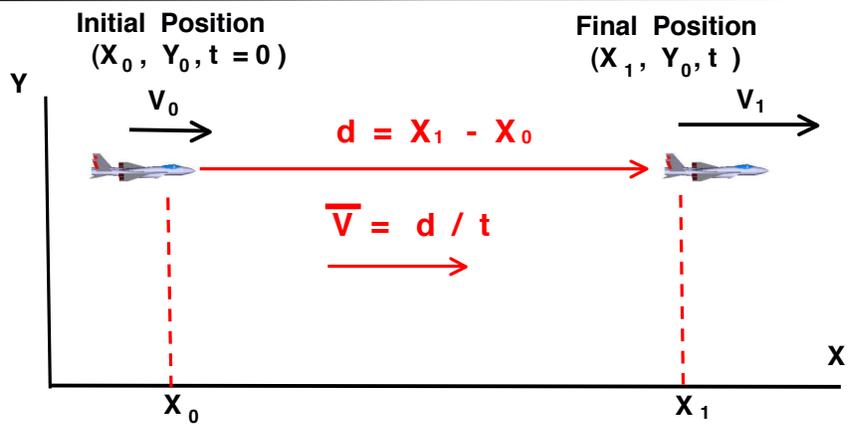
14

How do we describe motion?



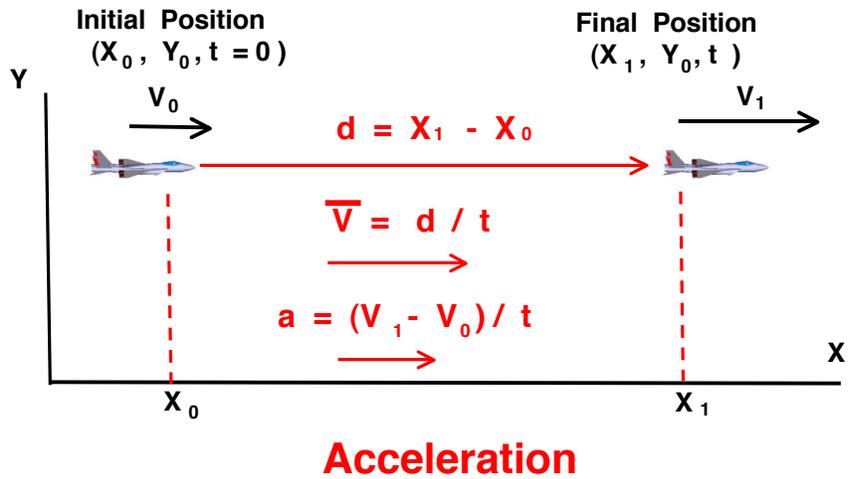
Displacement

How do we describe motion?



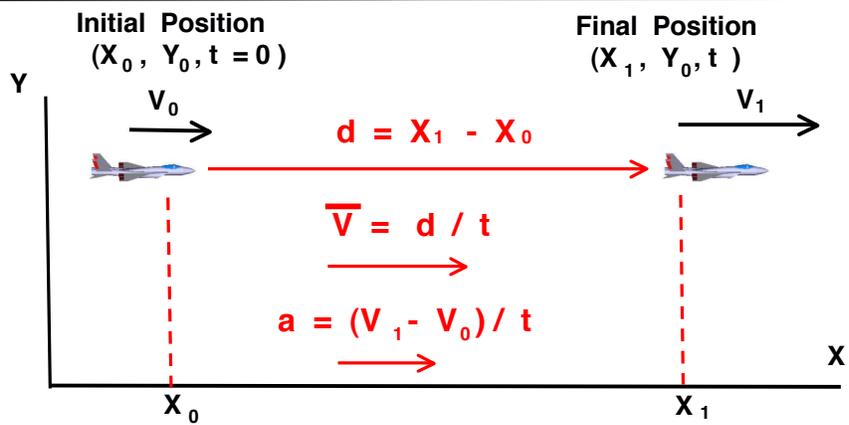
Average Velocity

How do we describe motion?



17

Displacement, Velocity, Acceleration

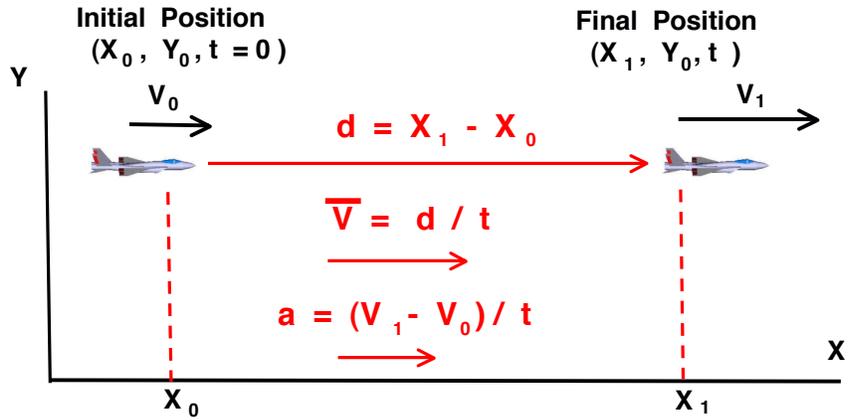


If velocity is constant - acceleration is zero

If acceleration is zero - velocity is constant

18

Displacement, Velocity, Acceleration



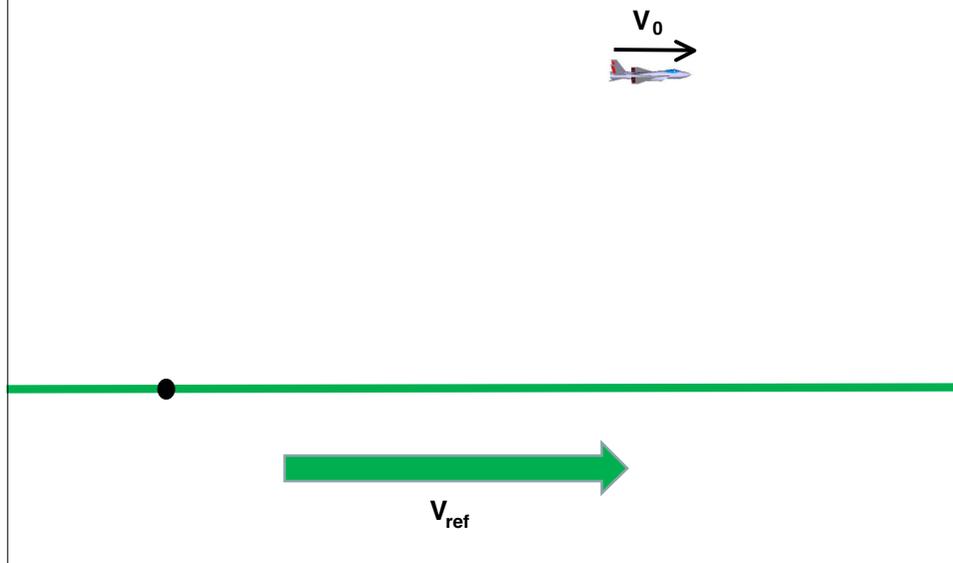
If the acceleration is a constant - $V_1 = V_0 + a t$

$$\bar{V} = \frac{1}{2} (V_1 + V_0) = \frac{1}{2} (V_0 + a t + V_0) = V_0 + \frac{1}{2} a t$$

$$d = t \bar{V} = V_0 t + \frac{1}{2} a t^2$$

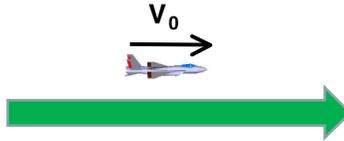
19

Suppose the Origin is Moving ?



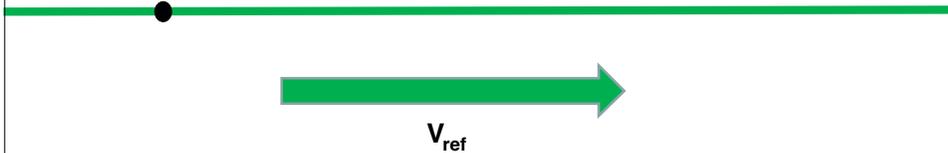
Suppose the Origin is Moving ?

Actual velocity of aircraft is
 $V_0 + V_{ref}$



If the reference velocity is constant – no problem

“Newtonian reference plane”



FORCE ?

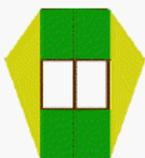
Glenn
Research
Center

What is it?

Why is it important?

What does it do ?

How does it work?



Examples ?





Forces

Glenn
Research
Center

Objects generate forces.
(objects are solid, liquid, or gas)

Forces cause motion.

Forces produce **acceleration.**

An object's mass **resists motion.**
(for the same force, heavier object accelerates less)

Forces come in pairs.



Newton's Laws of Motion

Glenn
Research
Center



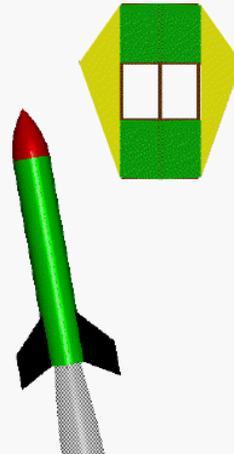
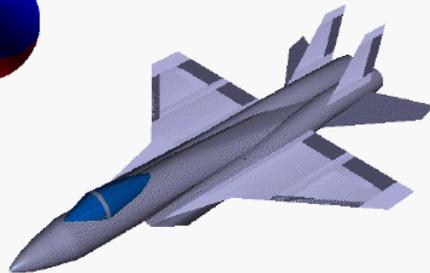
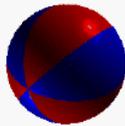
Sir Isaac Newton



Newton's First Law

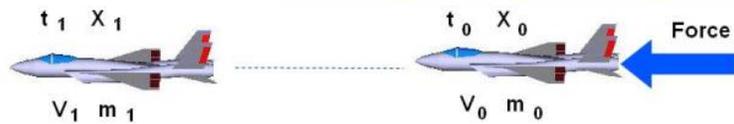
Glenn
Research
Center

"Every object persists in its state of rest or uniform motion in a straight line unless it is compelled to change that state by forces impressed on it."



National Aeronautics and Space Administration

Newton's Second Law



Force = Change of Momentum with Change of Time

Difference form:
$$F = \frac{m_1 V_1 - m_0 V_0}{t_1 - t_0}$$

t = time
X = location
m = mass
V = Velocity

With constant mass:
$$F = m \frac{V_1 - V_0}{t_1 - t_0}$$

$$F = m a$$

Force = mass x acceleration

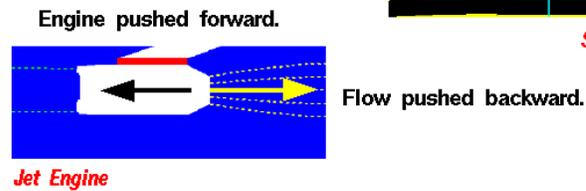
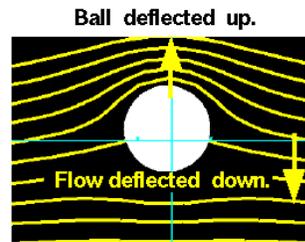
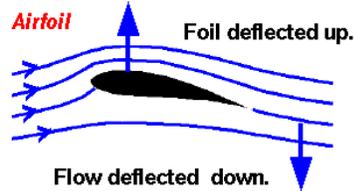
Velocity, acceleration, momentum and force are vector quantities



Newton's Third Law Applied to Aerodynamics

Glenn
Research
Center

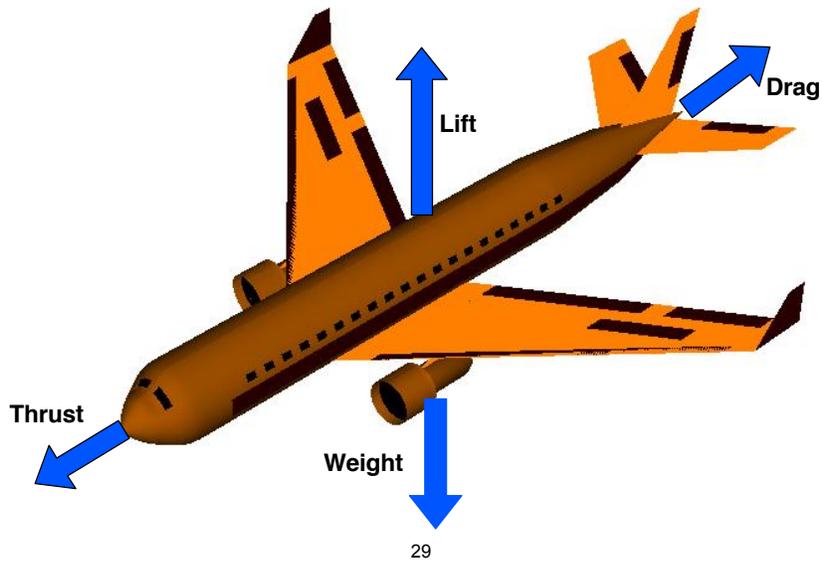
For every action, there is an equal and opposite re-action.



Tonight's Agenda

- 1) Quick review of last week
- 2) Lesson on Force and Motion
- 3) Experiments on Force and Motion**
- 4) More discussion on Post Project
- 5) Volunteers for Holiday Party

Four Forces on an Airplane



29



The Weight Equation

Glenn
Research
Center



In general: $F = G \frac{m_1 m_2}{d^2}$

Force equals a gravitational constant times the product of the masses divided by the square of the distance between the masses.

$$g = G \frac{m_{\text{earth}}}{d^2_{\text{earth}}} = 9.8 \frac{\text{meter}}{\text{sec}^2} = 32.2 \frac{\text{feet}}{\text{sec}^2}$$

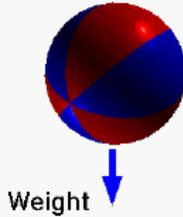
$$W = m g$$

Weight equals mass times gravitational acceleration.



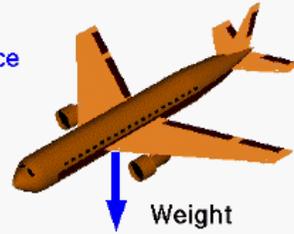
Free Falling Objects (no air resistance)

Glenn
Research
Center



Weight is the only Force acting on the object.

$$F = W = m g$$



Motion of the object (Newton's second law).

$$F = m a$$

$$a = \frac{F}{m} = \frac{W}{m} = \frac{m g}{m}$$

$$a = g$$

Mass of the object does not affect the motion.

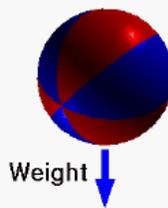
Shape of the object does not affect the motion.

All objects fall at the same rate in a vacuum. -- Galileo.



Motion of Free Falling Object (no air resistance)

Glenn
Research
Center



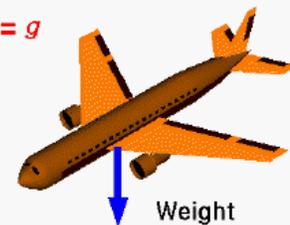
Constant Acceleration = g

V = velocity

X = distance

$$a = 9.8 \text{ m/sec}^2$$

$$V = a t \quad X = \frac{a t^2}{2}$$



Mass and shape of object does not affect the motion.

All objects fall at the same rate in a vacuum. -- Galileo.

Time - sec.	0	1	2	3	4	5	6	7	8
Accel - m/sec ²	9.8	9.8	9.8	9.8	9.8	9.8	9.8	9.8	9.8
Velocity - m/sec	0	9.8	19.6	29.4	39.2	49.	58.8	68.6	78.4
Dist - meters	0	4.9	19.6	44.1	78.4	122.5	176.4	240.1	313.6

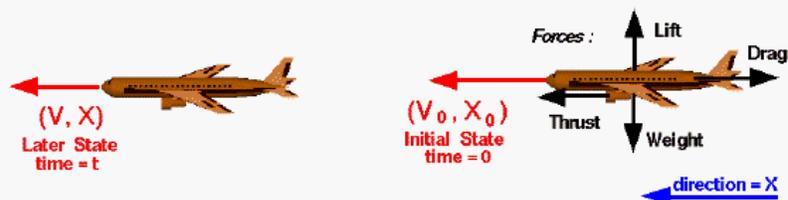
Tonight's Agenda

- 1) Quick review of last week
- 2) Lesson on Force and Motion
- 3) Experiments on Force and Motion
- 4) More discussion on Post Project
- 5) Volunteers for Holiday Party



Aircraft Motion – Constant Force *X* – Direction Only

Glenn
Research
Center



Newton's Second Law: $F = m a$ $F = \text{Force} = \text{Thrust} - \text{Drag}$
 $a = F / m$ $m = \text{Mass}$
 $a = \text{Acceleration}$
 $V = \text{Velocity}$

*If Force remains constant
acceleration is constant:*

$$V = a t + V_0$$
$$X = \frac{a t^2}{2} + V_0 t + X_0$$



On-Line Educational Resources

Glenn
Research
Center

Aerodynamics:

<http://www.grc.nasa.gov/WWW/K-12/airplane>

Wright Brothers:

<http://wright.nasa.gov/>

Aero Activities:

<http://www.grc.nasa.gov/WWW/K-12/aerores.htm>

Help:

Thomas.J.Benson@nasa.gov